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1. Solve

a)
$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{x^2}{y^2}$$

b)
$$\frac{\mathrm{d}y}{\mathrm{d}x} = x^3 y^2$$

c)
$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{\sin x}{\cos y}$$

2. Show that the differential equations

a)
$$(xy^2 + y)dx + (x^2y + x)dy = 0$$

b)
$$(e^x \sin y + 2x) dx + (e^x \cos y + 2y) dy = 0$$

are exact and solve them. (It is sufficient to give the solution to the latter equation in implicit form.)

3. Solve initial value problems

a)
$$y' = x^3(1-y)$$
, when $y(0) = 3$,

b)
$$y' = 2\sqrt{y+1} \cos x$$
, when $y(\pi) = 0$.

4. Find general solutions to equations

a)
$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{y}{x} + 2x + 1$$

$$b) \frac{\mathrm{d}y}{\mathrm{d}x} - y = e^{3x}$$

$$c) \frac{\mathrm{d}y}{\mathrm{d}x} - x - y - 1 = 0$$