

1. Let us consider a step potential and use the same notation as in the lecture notes. Calculate the coefficient  $B$  appearing in the wave function by using the continuity of the logarithmic derivative at the boundary point  $x = 0$ . Does the continuity of the logarithmic derivative determine the coefficient  $C$  also?
2. A particle having energy  $E$  scatters from a one-dimensional potential step of height  $V_0 < E$ .
  - a) Show that the probability density oscillates in region I, but is a constant in region II (use the same region numbering as in the lectures).
  - b) What is the wave length of the oscillations?
3. Show that the free particle Hamiltonian has eigenfunctions which are neither symmetric nor antisymmetric. Does this somehow contradict the proven statement: *If the potential in a one-dimensional Schrödinger equation is symmetric and an eigenfunction is non-degenerate, then the eigenfunction is either symmetric or antisymmetric.*
4. Show that a one-dimensional finite potential well always has at least one bound state.  
*Hint: One version of the proof is based on the intermediate value theorem.*
5. An electron is in the ground state of a one-dimensional potential well. The depth of the potential well is 2 eV and the width 1 Å. What is the binding energy of the electron?