Statistical physics

Problem set 12

- 1. Calculate the leading small- $T(O(T^2))$ correction to Pauli's paramagnetism. Sketch the behaviour of $\chi(T)$ when $0 \leq T < \infty$ and show that $\chi(T \to \infty)$ approaches the Curie law.
- 2. Derive the following expressions for the virial coefficients in terms of cluster integrals b_l :

$$B_2 = -b_2 = \frac{1}{2} \int d\mathbf{r} [1 - e^{-\beta v(r)}]$$
(1)

$$B_3 = 4b_2^2 - 2b_3 \tag{2}$$

$$B_4 = -20b_2^3 + 18b_2b_3 - 3b_4 \tag{3}$$

Calculate the 2nd virial coefficient for a gas of hard spheres $(v(r < d) = \infty, v(r \ge d) = 0)$ and a gas with a hard core and attractive "box"-potential $v(r < d) = \infty, v(d \le r < R) = -a, v(r \ge R) = 0.$

- 3. Consider 1-dimensional gas of hard "spheres", diameter d. N particles are moving along a line of length L. Determine the equation of state in the thermodynamic limit $N \to \infty$, $L \to \infty$ and N/L = constant. Does the system have phase transitions?
- 4. (*Extra if you have time:*) Calculate the isothermal compressibility $\kappa_{T,N}$ and and heat expansion coefficient $\alpha_{p,N}$ of low-temperature almost-degenerate fermi gas. What is C_p ?